

Name:	 <b>UPES</b> UNIVERSITY WITH A PURPOSE
Enrolment No:	

**UNIVERSITY OF PETROLEUM AND ENERGY STUDIES**  
**End Semester Examination, December 2019**

**Course: Advanced Thermodynamics**

**Program: MTech (CE+PD)**

**Course Code: CHPD 7003**

**Semester: 1**

**Time 03 hrs.**

**Max. Marks: 100**

**Instructions:**

1. The exam is closed book and closed notes
2. Use of mobile phone and other electronic equipment is strictly prohibited
3. Use of unfair means during exam will be severely dealt with.

**SECTION A**

S. No.		Marks	CO
Q 1	Write down the enthalpy form of the fundamental property relation from combined first and second law.	4	CO1
Q 2	Express $\left(\frac{\partial T}{\partial P}\right)_S$ in terms of specific heats and P-V-T relations.	4	CO2
Q 3	Define excess volume of a mixture. How is it related to the activity coefficient?	4	CO3
Q 4	A system initially containing 5 moles of C <sub>2</sub> H <sub>4</sub> and 8 moles of O <sub>2</sub> undergo the multiple reactions: $C_2H_4(g) + 1/2 O_2(g) \rightarrow ((CH_2)_2O(g))$ $C_2H_4(g) + 3 O_2(g) \rightarrow CO_2(g) + 2H_2O(g)$ Develop expressions for the mole fraction of the reacting species as a function of the reaction coordinate of the two reactions.	4	CO4
Q 5	State the relation between entropy and probability of microstates in a canonical ensemble.	4	CO5

**SECTION B**

Q 6	A heat engine operating in outer space may be assumed equivalent to a Carnot engine operating between reservoirs at temperatures $T_H$ and $T_C$ . The only way the heat can be discarded from the engine is by radiation, the rate of which is given approximately by the equation, $ \dot{Q}_C  = kAT_C^4$ where $k$ is a constant and $A$ is the area of the radiator. Prove that, for a fixed power output $ \dot{W} $ and for fixed temperature $T_H$ , the radiator area is a minimum when the temperature of the cold to the heat reservoir is 0.75.	10	CO1
Q 7	Determine expressions for $G^R$ and $U^R$ as implied by the van der Waals' equation of state	10	CO2
Q 8	Show that, $\gamma_i = \hat{\phi}_i / \phi_i$ where the symbols have their usual meanings.	10	CO3

Q 9	<p>The canonical partition function of a monoatomic ideal gas is given by the formula,</p> $Q(N, V, T) = \frac{1}{N!} \left( \frac{2\pi m k_B T}{h^2} \right)^{3N/2} V^N$ <p>where,  <math>N</math> = total number of particles present,  <math>m</math> = mass of each particle,  <math>T</math> = temperature of the system,  <math>V</math> = volume of the system,  <math>h</math> = Planck's constant.  Find expressions for the pressure and energy.</p>	10	CO5
<b>SECTION C</b>			
Q 10	<p>For ideal gases, exact mathematical expressions can be derived for the effect of temperature and pressure on the equilibrium conversion, <math>\varepsilon_e</math>. Show that:</p> $\left( \frac{\partial \varepsilon_e}{\partial T} \right)_P = \frac{K_y}{RT^2} \frac{d\varepsilon_e}{dK_y} \Delta H^\circ$ $\left( \frac{\partial \varepsilon_e}{\partial P} \right)_T = \frac{K_y}{P} \frac{d\varepsilon_e}{dK_y} (-\nu)$ <p>where the symbols have their usual meanings.</p>	20	CO4
Q 11	Derive expressions for the probabilities of different microstates in the case of a grand canonical ensemble.	20	CO5