

Name:	
Enrolment No:	

**UNIVERSITY OF PETROLEUM AND ENERGY STUDIES**  
**End Semester Examination, December 2019**

**Course: Theory of Elasticity & Plasticity**  
**Program: M.Tech. Structural Engineering**  
**Course Code: CIVL 7002**

**Semester: I**  
**Time 03 hrs.**  
**Max. Marks: 100**

**Instructions: Answer all questions of Section A, B & C**  
**(Assume all the necessary data if necessary) (Internal Choice is there in Q 5-Section B and Q 6-Section C)**

**SECTION A**

S. No.		Marks	CO
Q 1	Prove the following Airy's stress functions and examine the stress distribution represented by them: a) $\Phi = Ax^2 + By^2$ b) $\Phi = Ax^3$ c) $\Phi = A(x^4 - 3x^2y^2)$ d) $\Phi = A(x^3 - 3x^2y^2)$ e) $\Phi = Ax^2y^2$	4 4 4 4 4	CO2

**SECTION B**

Q 2	The stress components at a point are given by the following array: $\begin{bmatrix} 10 & 5 & 6 \\ 5 & 8 & 10 \\ 6 & 10 & 6 \end{bmatrix} MPa$ Calculate the Principal Stresses and Principal Planes.	10	CO1
Q 3	Using Polynomials, calculate the bending of cantilever beam loaded at the end.	10	CO2
Q 4	Develop Constitutive matrix for Tetragonal material. Using direction cosine matrix, Stress matrix, obtain number of elastic constants.	10	CO1
Q 5	Define different hardening rules for materials in case of plastic state. <u>Or</u> Obtain yield criteria of metals graphically in case of plastic state.	10	CO4

**SECTION-C**

Q 6	An elliptical shaft of semi axis $a = 0.05m$ , $b = 0.025m$ , and $G = 80 GPa$ is subjected to a twisting moment of $1200 \Pi N m$ . Determine the maximum shearing stress and the angle of twist per unit length. <u>Or</u> Calculate torsional rigidity for elliptical section using stress function approach.	20	CO3
Q 7	A load $P = 70 kN$ is applied to the circular steel frame shown in the figure. The rectangular cross section is $0.1m$ wide and $0.05m$ thick. Determine the tangential stress at point A and B	20	CO3

