

Roll No: -----



UNIVERSITY OF PETROLEUM AND ENERGY STUDIES

End Semester Examination, May 2018

Programme: B. Plan.

Course Name: Statistical and Quantitative Methods in Planning-II

Course Code: MATH 1007

No. of page/s: 02

Semester – II

Max. Marks : 100

Duration : 3 Hrs

Instructions:

Attempt all questions from **Section A** (each carrying 4 marks); attempt all questions from **Section B** (each carrying 8 marks); attempt **Section C** (each carrying 20 marks).

Section A
(All questions are compulsory)

1.	Explain the properties of correlation coefficient.	[4]	CO1
2.	Define feasible solution, infeasible solution and basic feasible solution.	[4]	CO2
3.	Describe the components of decision making.	[4]	CO4
4.	Write all the conditions to apply the ANOVA.	[4]	CO3
5.	Discuss the properties and conditions for chi-square test.	[4]	CO3

SECTION B
(Q6, Q7, Q8, Q9 are compulsory and Q10 has internal choices)

6.	Calculate the coefficient of correlation between x and y for the following data							[8]	CO1	
	x :	65	66	67	68	69	70			71
	y :	67	68	66	69	72	72			69
7.	A stenographer claims that she can type at the rate of 120 words per minute. Can we reject her claim on the basis of 100 trials in which she demonstrates a mean of 116 words with a standard deviation of 15 words? Use 5% level of significance. (Given $Z_{0.05}=1.96$)							[8]	CO3	
8.	Find out the regression coefficient of Y on X from the following data:							[8]	CO1	
	X	1	2	3	4	5				
	Y	160	180	140	180	200				

9.	<p>The following table gives the number of accidents that occurred during the various days of the week. Find whether the accidents are uniformly distributed over the week. (Given $\chi^2_{6, 0.05}=12.59$)</p> <table border="1" data-bbox="228 344 1268 422"> <tr> <td>Days</td> <td>Sun.</td> <td>Mon.</td> <td>Tue.</td> <td>Wed.</td> <td>Thu.</td> <td>Fri.</td> <td>Sat.</td> </tr> <tr> <td>No. of Accidents</td> <td>14</td> <td>16</td> <td>8</td> <td>20</td> <td>11</td> <td>9</td> <td>14</td> </tr> </table>	Days	Sun.	Mon.	Tue.	Wed.	Thu.	Fri.	Sat.	No. of Accidents	14	16	8	20	11	9	14	[8]	CO3														
Days	Sun.	Mon.	Tue.	Wed.	Thu.	Fri.	Sat.																										
No. of Accidents	14	16	8	20	11	9	14																										
10.	<p>Use the graphical method to solve the following LP problem</p> <p style="text-align: center;">$\text{Max. } Z = 15x_1 + 10x_2$</p> <p>subject to the constraints</p> <p style="text-align: center;">$4x_1 + 6x_2 \leq 360$</p> <p style="text-align: center;">$3x_1 \leq 180$</p> <p style="text-align: center;">$5x_2 \leq 200$</p> <p style="text-align: center;">$x_1, x_2 \geq 0$</p> <p style="text-align: center;">OR</p> <p>Define Basic solution and optimum basic feasible solution with an example.</p>	[8]	CO2																														
<p>SECTION C</p> <p>(Q11.A, Q11.B are compulsory and Q12 has internal choices)</p>																																	
11.A	<p>Ruth and Charlie play a game. At each play, Ruth and Charlie simultaneously extend either one or two fingers and call out a number. The player whose call equals the total number of extended fingers wins that many pennies from the opponent. In the event that neither player's call matches the total, no money changes hands.</p> <p>i) Write down a pay-off matrix for this game (here the strategy (1, 2) means that the player holds up one finger and shouts 2).</p> <p>ii) What is the payoff for Ruth if Ruth shows two fingers and calls out 4 and Charlie shows 1 finger and calls out 3? What is the payoff for Charlie in this situation?</p>	[10]	CO4																														
11.B	<p>A company has three production facilities S_1, S_2 and S_3 with production capacity 7, 9 and 18 units per week of a product, respectively. These units are to be shipped to four warehouses D_1, D_2, D_3 and D_4 with requirement of 5, 6, 7 and 14 units per week, respectively. The transportation costs per unit (in rupees) between factories to warehouses are given in the following table:</p> <table border="1" data-bbox="228 1619 1268 1808"> <tr> <td></td> <td>D_1</td> <td>D_2</td> <td>D_3</td> <td>D_4</td> <td>Capacity</td> </tr> <tr> <td>S_1</td> <td>19</td> <td>30</td> <td>50</td> <td>10</td> <td>7</td> </tr> <tr> <td>S_2</td> <td>70</td> <td>30</td> <td>40</td> <td>60</td> <td>9</td> </tr> <tr> <td>S_3</td> <td>40</td> <td>8</td> <td>70</td> <td>20</td> <td>18</td> </tr> <tr> <td>Demand</td> <td>5</td> <td>8</td> <td>7</td> <td>14</td> <td>34</td> </tr> </table> <p>Solve this transportation problem.</p>		D_1	D_2	D_3	D_4	Capacity	S_1	19	30	50	10	7	S_2	70	30	40	60	9	S_3	40	8	70	20	18	Demand	5	8	7	14	34	[10]	CO2
	D_1	D_2	D_3	D_4	Capacity																												
S_1	19	30	50	10	7																												
S_2	70	30	40	60	9																												
S_3	40	8	70	20	18																												
Demand	5	8	7	14	34																												

12	<p>The three samples below have been obtained from normal populations with equal variances. Test the hypothesis at 5% level that the population means are equal:</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 2px 10px;">8</td> <td style="padding: 2px 10px;">7</td> <td style="padding: 2px 10px;">12</td> </tr> <tr> <td style="padding: 2px 10px;">10</td> <td style="padding: 2px 10px;">5</td> <td style="padding: 2px 10px;">9</td> </tr> <tr> <td style="padding: 2px 10px;">7</td> <td style="padding: 2px 10px;">10</td> <td style="padding: 2px 10px;">13</td> </tr> <tr> <td style="padding: 2px 10px;">14</td> <td style="padding: 2px 10px;">9</td> <td style="padding: 2px 10px;">12</td> </tr> <tr> <td style="padding: 2px 10px;">11</td> <td style="padding: 2px 10px;">9</td> <td style="padding: 2px 10px;">14</td> </tr> </table> <p>(The table value of F at 5% level of significance for $\nu_1=2$ and $\nu_2=12$ is 3.88)</p> <p style="text-align: center;">OR</p> <p>The following table gives the yield on 15 sample fields under three varieties of seeds (<i>viz.</i>, A, B, C).</p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 2px 10px;">A</th> <th style="padding: 2px 10px;">B</th> <th style="padding: 2px 10px;">C</th> </tr> </thead> <tbody> <tr> <td style="padding: 2px 10px;">20</td> <td style="padding: 2px 10px;">18</td> <td style="padding: 2px 10px;">25</td> </tr> <tr> <td style="padding: 2px 10px;">21</td> <td style="padding: 2px 10px;">20</td> <td style="padding: 2px 10px;">28</td> </tr> <tr> <td style="padding: 2px 10px;">23</td> <td style="padding: 2px 10px;">17</td> <td style="padding: 2px 10px;">22</td> </tr> <tr> <td style="padding: 2px 10px;">16</td> <td style="padding: 2px 10px;">25</td> <td style="padding: 2px 10px;">28</td> </tr> <tr> <td style="padding: 2px 10px;">20</td> <td style="padding: 2px 10px;">15</td> <td style="padding: 2px 10px;">32</td> </tr> </tbody> </table> <p>Test at 5% level of significance whether the average yields of land under different varieties of seeds show significant differences. Table value of F at 5% level for $\nu_1=2$ and $\nu_2=12$ is 3.88)</p>	8	7	12	10	5	9	7	10	13	14	9	12	11	9	14	A	B	C	20	18	25	21	20	28	23	17	22	16	25	28	20	15	32	[20]	CO3
8	7	12																																		
10	5	9																																		
7	10	13																																		
14	9	12																																		
11	9	14																																		
A	B	C																																		
20	18	25																																		
21	20	28																																		
23	17	22																																		
16	25	28																																		
20	15	32																																		

Roll No: -----



UNIVERSITY OF PETROLEUM AND ENERGY STUDIES

End Semester Examination, May 2018

Programme: B. Plan.

Course Name: Statistical and Quantitative Methods in Planning-II

Course Code: MATH 1007

No. of page/s: 02

Semester – II

Max. Marks : 100

Duration : 3 Hrs

Instructions:

Attempt all questions from **Section A** (each carrying 4 marks); attempt all questions from **Section B** (each carrying 8 marks); attempt **Section C** (each carrying 20 marks).

Section A
(All questions are compulsory)

1.	Explain Merits and limitations of rank correlation coefficient.	[4]	CO1
2.	Define Basic solution and optimum basic feasible solution.	[4]	CO2
3.	Describe the various environments for decision making.	[4]	CO4
4.	Write all the conditions to apply the ANOVA.	[4]	CO3
5.	Discuss the applications of chi-square test.	[4]	CO3

SECTION B
(Q6, Q7, Q8, Q9 are compulsory and Q10 has internal choices)

6.	Calculate the coefficient of correlation between Marks in Physics and Marks in Chemistry for the following data						[8]	CO1		
	<i>Marks in Physics</i>	65	66	67	68	69			70	71
	<i>Marks in Chemistry</i>	67	68	66	69	72			72	69
7.	Ten objects are chosen at random from a large population and their weights are found to be in gms: 63, 63, 64, 65, 66, 69, 69, 70, 70, and 71. In the light of this data, discuss the suggestion that the mean weight in the universe is 65 gms. (Given $t_{0.05, 9}=2.262$)						[8]	CO3		
8.	Find out the regression coefficient of Y on X from the following data:						[8]	CO1		
	X	2	4	6	8	10				
	Y	16	18	14	18	20				

9.	The following table gives the number of births that occurred during the various days of the week. Find whether the births are uniformly distributed over the week.							[8]	CO3	
	Days	Sun.	Mon.	Tue.	Wed.	Thu.	Fri.			Sat.
	No. of births	4	6	8	2	1	9			4

(Given $\chi^2_{6, 0.05}=12.59$)

10.	Use the graphical method to solve the following LP problem $\text{Max. } Z = 3x_1 + 2x_2$ Subject to the constraints $4x_1 + 6x_2 \leq 36$ $3x_1 \leq 18$ $5x_2 \leq 20$ $x_1, x_2 \geq 0$	[8]	CO2
	OR		
Define feasible solution, infeasible solution and basic feasible solution with an example.			

SECTION C
(Q11.A, Q11.B are compulsory and Q12 has internal choices)

11.A	A producer of boats has estimated the following distributions of demand for a particular kind of boat:							[10]	CO4	
	No. Demanded	0	1	2	3	4	5			6
	Probability	0.14	0.27	0.27	0.18	0.09	0.04			0.01

Each boat cost him Rs. 7000 and he sells them for Rs. 10000 each. Any boat that is left unsold must be disposed off for Rs. 6000 each. How many boats should be in stock so as to maximize his expected profit?

11.B	A company has three production facilities S_1, S_2 and S_3 with production capacity 8, 10 and 12 units per week of a product, respectively. These units are to be shipped to four warehouses D_1, D_2, D_3 and D_4 with requirement of 7, 8, 10 and 5 units per week, respectively. The transportation costs per unit (in rupees) between factories to warehouses are given in the following table:						[10]	CO2
		D_1	D_2	D_3	D_4	Capacity		
	S_1	19	30	50	10	8		
	S_2	70	30	40	60	10		
	S_3	40	8	70	20	12		
	Demand	7	8	10	5	30		

Solve this transportation problem.

The three samples below have been obtained from normal populations with equal variances. Test the hypothesis at 5% level that the population means are equal:

8	7	12
10	5	9
7	10	13
14	9	12
11	9	14

(The table value of F at 5% level of significance for $\nu_1=2$ and $\nu_2=12$ is 3.88)

OR

The following table gives the yield on 15 sample fields under three varieties of seeds (*viz.*, A, B, C).

A	B	C
20	18	25
21	20	28
23	17	22
16	25	28
20	15	32

Test at 5% level of significance whether the average yields of land under different varieties of seeds show significant differences.

(Table value of F at 5% level for $\nu_1=2$ and $\nu_2=12$ is 3.88)

12.

[20]

CO3